

## Common Formulae

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### DNA:

1 A260 = 0.05 µg DNA/µL

A260 /A280 = 2.0

Å =  $6.02 \times 10^{23}$  molecules/mole

1 haploid human genome =  $3.2 \times 10^9$  bp

Avg MW of DNA = 654 Dal/bp (1 Dalton = 1 gm/mole)

1 cell = 7 pg genomic DNA

### Protein

Mouse Ig heavy chain = 52 kD

Mouse cyclin A2 = 47 kD

Mouse CDK2 = 39 kD

Mouse Ig lambda light chain = 26 kK

### $\lambda$ + HindIII

(kB)	23.130	9.416	6.557	4.361	2.322	2.027	0.564	0.125
(fraction of total)	0.477	0.194	0.135	0.090	0.478	0.418	0.0116	0.0028

### Bacteria:

$10^9$  bacteria/mL = 1 A<sub>600</sub>

### Relative centrifugal force (g):

$RCF = 1.12 R(\text{rpm}/1000)^2$

$\text{rpm} = 948\sqrt{RCF / R}$

(where R = radius in mm)

**Radiation:**

Measurement	International (SI) Unit	U.S. Unit	Conversions
Radioactivity	Becquerel (Bq)	Curie (Ci)	3.7E+10 Bq = 1 Ci)
Absorbed Dose	Gray (Gy)	RAD	1 Gy = 100 RADs
Equivalent Dose	Sievert (Sv)	REM	1 Sv = 100 REMs

1 Bq = 1 dps (disintegrations per second)

1 Ci = dps/ dps in 1 gm radium

1 Gy = 1 J/kg (Joules absorbed per kg of target liquid or gas)

**Radiation dose:***Relationships*

1 R (Röntgen) = ionizing energy emitted in air

1R @1 rad (radiation absorbed dose in a liquid or gas)

1 Sv = Q x Gy

1 rem = Q x rad (rem = Röntgen equivalents in man)

(Q = "quality score" ~ 1 for  $\beta$  particles.)

To convert radioactivity to dose (e.g. 1 Ci <sup>32</sup>P in 1 L H<sub>2</sub>O)

1 Ci = 4.12E-03 W / 1 kg  
= 4.12E-03 Gy/sec

**Characteristics of common radionuclides in biology labs:**

Nuclide	Atomic Number	Half Life	Principal Mode(s) of Decay	Major radiation Energies (MeV/dis)			(W/Ci)
				$\alpha$	$\beta -$	$\gamma$ and X	
<sup>3</sup> H	1	1.233E+01 yr	$\beta -$		0.00568		3.37E-05
<sup>14</sup> C	6	5.730E+03 yr	$\beta -$		0.0495		2.93E-04
<sup>32</sup> P	15	14.282 days	$\beta -$		0.6947		4.12E-03
<sup>35</sup> S	16	87.51 days	$\beta -$		0.0486		2.88E-04
<sup>125</sup> I	53	60.14 days	EC		0.0179	0.0423	3.57E-04
<sup>131</sup> I	53	8.040 days	$\beta -$		0.1913	0.3826	3.40E-03

**Radiation risk:**

Avg U.S. background radiation exposure = 0.36 rem

Maximum annual occupational dose = 5 rem

4 Sv causes a doubling of total cancer risk (baseline = 0.22)

1 Sv causes a doubling of leukemia risk (baseline = 0.0063)

**References:**

<http://www.umich.edu/~radinfo/>

<http://www.radtexas.org/radunits.html>

## Sample variance:

*Measures of Variance:*

$$V = \sigma^2 = \sum_{i=1}^n \frac{|x - \mu|^2}{n} \quad (\text{where } \mu = \text{true population mean, } \sigma = \text{population S.D.})$$

For Gaussian (bell shaped) distributions,  $\mu \pm \sigma$  are the inflections points of the curve, i.e. where it becomes concave with  $d^2P/dx^2 = 0$ , and the area under the probability curve = 68%.

*Sample variance:*

$$s^2 = \sum_{i=1}^n \frac{|x_i - X|^2}{n - 1}$$

*Variance for a linear transformation of x:*

$$y = mx + b$$

(where m = slope, b = y-intercept)

$$\sigma_y = m\sigma_x$$

*Variance of multiple measurements:*

*For addition*

$$V_{(x+y)} = V_x + V_y \quad (\text{the variance is additive})$$

i.e.

$$s_{(x+y)} = \sqrt{s_x^2 + s_y^2}$$

*For multiplication*

$$\frac{V_{xy}}{\mu_x \mu_y} = \frac{V_x}{\mu_x^2} + \frac{V_y}{\mu_y^2} \quad (\text{the relative variance is additive})$$

i.e.

$$s_{xy} = \sqrt{\left( \frac{s_x^2}{\mu_x^2} + \frac{s_y^2}{\mu_y^2} \right)} (\mu_x \mu_y) \quad (\text{O.K., I admit that I'm guessing here})$$

### **Poisson distributions**

$$P(x) = \frac{e^{-\mu} \mu^x}{x!}$$

$P(1) = e^{-\mu} \mu$  (the first element of the Poisson, i.e. the probability of 1 event per observation)

The probabilities of even or odd numbers of events:

$P(x_{odd}) = 1/2(1 - e^{-2\mu})$  (for example the probability of 1,3,5... SCE per chromosome)

$$P(x_{even}) = 1/2(1 + e^{-2\mu})$$

Variance:

$$\mu_x = s_x^2 \quad (\text{for Poisson distributions the mean} = \text{variance})$$

## Sample size determination

For numerical data, comparing one group to a known standard:

$$n = \left[ \frac{(z_\alpha - z_\beta)\sigma}{\mu_x - \mu} \right]^2$$

(where  $z_\alpha$  and  $z_\beta$  are the z-values for type 1 or type 2 errors,  $\sigma$  is the std. Deviation of the population and  $\mu$  is the true population mean.)

For numerical data, comparing 2 groups to each other:

$$n = 2 \left[ \frac{(z_\alpha - z_\beta)\sigma}{\mu_x - \mu} \right]^2$$

e.g. let  $\alpha=0.95$ ,  $\beta=0.8$ ,  $z_\alpha=1.96$ ,  $z_\beta=-1.28$

$$n = \frac{21\sigma^2}{(\mu_x - \mu)^2}$$

For ordinal (true/false) data comparing the proportions of two groups to each other, the  $X^2$  gives:

$$n = \left[ \frac{z_\alpha \sqrt{2(\pi_c - \pi_c^2)} - z_\beta \sqrt{(\pi_x - \pi_x^2) + (\pi_c - \pi_c^2)}}{\pi_x - \pi_c} \right]^2$$

(where  $\pi_c$  is the control frequency, and  $\pi_x$  is the experimental frequency)

e.g. for  $\alpha=0.05$ , and  $1-\beta=0.8$ :

n	$\pi_c$	$\pi_x$
50	0.33	0.66
24	0.25	0.66
10	0.20	0.80